

Iteratively Composing Statically Verified Traits

Can metaprogramming generate statically verified code reusing common verification techniques?

Isaac Oscar Gariano¹

Marco Servetto¹

Alex Potanin¹

Hrshikesh Arora¹

¹Victoria University of Wellington

```

@requires (exp > 0)
@ensures (result = x**exp)
Int pow(Int x, Int exp) {
  if (exp == 1) return x;
  if (exp %2 == 0) return pow(x*x, exp/2); //even
  return x*pow(x, exp-1); } //odd

```

If the exponent is known at compile time, unfolding the recursion produces even more efficient code:

```

@ensures (result = x**7) Int pow7(Int x) {
  Int x2 = x*x; // x**2
  Int x4 = x2*x2; // x**4
  return x*x2*x4; } // Since 7 = 1 + 2 + 4

```

- ▶ OO languages supporting static verification usually extends method declaration with syntax supporting pre/post conditions. During compilation, directly after typing, an automatic theorem prover checks the constraints.
- ▶ Very slow even on fast hardware!
- ▶ `pow(x, y)` execution is slower than an hand written `pow7(x)`
- ▶ Manually declaring `pown` methods: repetitive, boring.
- ▶ Running the static verifier on all `pown` versions: time consuming

Pow

What if we could programmatically generate code at compile time? For example, we could write `generate(y)` as a method generating a class body with a method `pow(x)` computing `pow(x, y)`

```
class Pow7: generate(7)
```

```
...
```

```
Pow7.pow(4) == pow7(4)
```

Iteratively building up pow

- ▶ Verification supports code reuse / class inheritance.
- ▶ What if metaprogramming was based on code reuse?
- ▶ For example, here we use inheritance to encode statically verified powers while reusing part of the already verified contract
- ▶ A code optimizer could inline nested calls, producing the same efficient code of the hand written versions of before

```
class Pow1{  
  @ensures (result=x**1)  
  Int pow1(Int x){return x;}  }
```

```
class Pow2 extends Pow1{  
  @ensures (result=x**2)  
  Int pow2(Int x){return x*pow1(x);}  }
```

```
class Pow3 extends Pow2{  
  @ensures (result=x**3)  
  Int pow3(Int x){return x*pow2(x);}  }
```

Pow and Exp

```
class Pow1{  
    Int exp1 () {return 1;}  
    @ensures (result=x**exp1 ())  
    Int pow1 (Int x) {return x;} }  
}
```

```
class Pow2 extends Pow1{  
    Int exp2 () {return exp1 ()+1;}  
    @ensures (result=x**exp2 ())  
    Int pow2 (Int x) {return x*pow1 (x);} }  
}
```

```
class Pow3 extends Pow2{  
    Int exp3 () {return exp2 ()+1;}  
    @ensures (result=x**exp3 ())  
    Int pow3 (Int x) {return x*pow2 (x);} }  
}
```

Traits

```
//induction base case: pow(x)=x**1
Trait base=class {
  @ensures(result>0)@ensures(result=1) Int exp() {return 1;}
  @ensures(result=x**exp()) Int pow(Int x) {return x;}
}
//if _pow(x)=x**_exp(), pow(x)=x**(1+_exp())
Trait odd=class {
  @ensures(result>0) Int _exp();
  @ensures(result=1+_exp()) Int exp() {return 1+_exp();}
  @ensures(result=x**_exp()) Int _pow(Int x);
  @ensures(result=x**exp()) Int pow(Int x) {return x*_pow(x);}
}
//if _pow(x)=x**_exp(), pow(x)=x**(2*_exp())
Trait even=class {
  @ensures(result>0) Int _exp();
  @ensures(result=2*_exp()) Int exp() {return 2*_exp();}
  @ensures(result=x**_exp()) Int _pow(Int x);
  @ensures(result=x**exp()) Int pow(Int x) {return _pow(x*x);}
}
```

Trait composition

```
// 'compose' performs a step of iterative composition
Trait compose(Trait current, Trait next) {
  current = current[rename exp()->_exp(), pow(x)->_pow(x)];
  return (current+next)[hide _exp(), _pow(x)];
}
```

```
@requires(exp>0) // the entry point for our metaprogramming
Trait generate(Int exp) {
  if (exp==1) return base;
  if (exp%2==0) return compose(generate(exp/2), even);
  return compose(generate(exp-1), odd);
}
```

```
class Pow7: generate(7)
// the body of class Pow7 is the result of generate(7)
```

```
/* example usage: */ new Pow7().pow(3) == 2187 // Compute 3**7
```


Comparing code

```
//conventional code
@requires(exp > 0)
@ensures(result = x**exp)
Int pow(Int x, Int exp) {
    if (exp == 1) return x;
    if (exp %2 == 0) return pow(x*x, exp/2); //even
    return x*pow(x, exp-1); } //odd

//metaprogramming
@requires(exp>0)
Trait generate(Int exp) {
    if (exp==1) return base;
    if (exp%2==0) return compose(generate(exp/2), even);
    return compose(generate(exp-1), odd);
}

class Pow7:{//generated code
    @ensures(result>0) exp(){return 1+1+1+1+1+1+1;}
    @ensures(result = x**exp()) Int pow(Int x) {??}
```

Concluding

- ▶ Idea: merge conventional verification and trait composition.
- ▶ Iterative composition (metaprogramming) allows to generate code that is correct by construction.
- ▶ Theorem prover/manual verification only for the basic building blocks.
- ▶ Contracts are syntactically matched during the sum operation.
- ▶ What is the contract of the result?
- ▶ We are searching for relevant related work!

Thanks

Questions?