



Towards the Verification of Refactorings of Hybrid Simulink Models

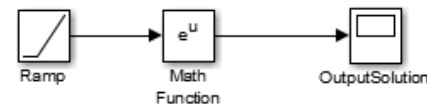
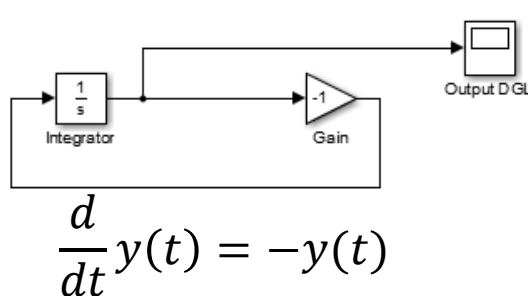
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Goal

Automated verification of refactorings of hybrid Simulink models

Example



Criteria

- Automated verification
- Transformation correctness
- Support for hybrid models
- Industrial relevance

Motivation

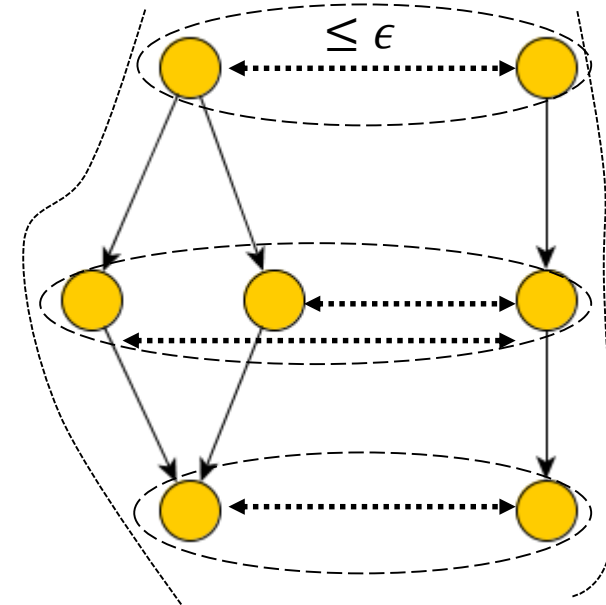
- Simulink de facto standard for Model Driven Engineering in Automotive, Aerospace etc.
- Verification esp. in safety-critical environments
- Refactorings improve structure, preserve behaviour



Related Work

	Simulink semantics	Simulink verification		Approximate Bisimulation	Simulink refactorings	Simulink refactorings verif.	Remarks
		Discrete Models	Hybrid Models				
Mathworks documentation	✓						Informal semantics
Bouissou, Chapoutot, ACM SIGPLAN 2012	✓						Formal semantics
Herber, EMSOFT 2013		✓					Transf. to UCLID
Caspi, ACM TECS 2005		✓					Transf. to LUSTRE
Reicherdt, Glesner, ICSE 2014		✓					Transf. to BOOGIE
Agrawal, Simon, Karsai, 2004			✓				Transf. to hybrid automata
Girard, Pappas, European Journal of Control, 2011				✓			
Tran, Wilmes, Dziobek, ICSEA 2013					✓		
Stuermer, Mathworks Automotive 2007					✓		
Our approach aims at	✓	✓	✓	✓	✓	✓	under development

- LTS $T_i = (Q_i, Q_i^0, \rightarrow_i, \Pi, \langle \cdot \rangle_i)$
- $B_\epsilon \subseteq Q_1 \times Q_2$
- B_ϵ approximate bisimulation of precision $\epsilon \Leftrightarrow \forall (q_1, q_2) \in B_\epsilon$:

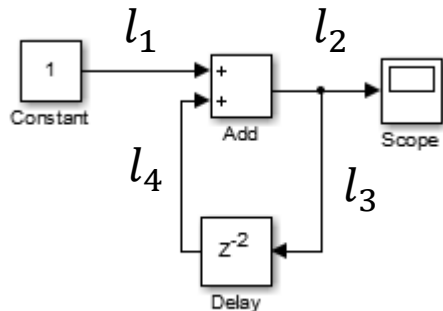


1. $d(\langle q_1 \rangle_1, \langle q_2 \rangle_2) \leq \epsilon$
2. $\exists q'_1: q_1 \rightarrow q'_1 \Rightarrow \exists q'_2: q_2 \rightarrow q'_2 \wedge (q'_1, q'_2) \in B_\epsilon$ and vice versa

- $T_1 \sim T_2 \Leftrightarrow \forall q_1 \in Q_1^0 \exists q_2 \in Q_2^0 \exists B_\epsilon \subseteq Q_1 \times Q_2$ approx. bisimulation relation: $(q_1, q_2) \in B_\epsilon$

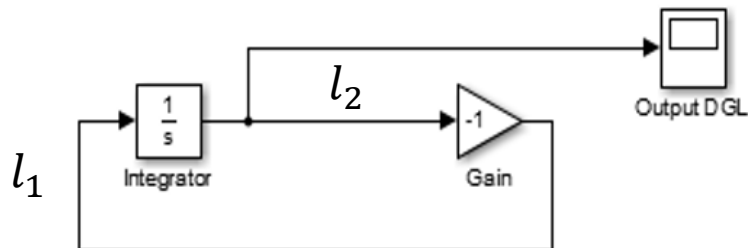
1. **Abstract Representation (AR)**:
Equation set describing how blocks modify signals
2. Proof of **soundness** of AR with operational semantics
3. Adaptation of **approximate bisimulation** as more suitable notion of equivalence than traditional bisimulation
4. **Epsilon tubes** for the precision of the approximate bisimulations

- **Equation set** that describes how the signal is modified at a block by relating input and output
- ⇒ Sound with semantics; enables abstraction



$$l_1(t) = 1, l_2(t) = l_1(t) + l_4(t),$$

$$l_3(t) = l_2(t), l_4(t + 2h) = l_3(t)$$



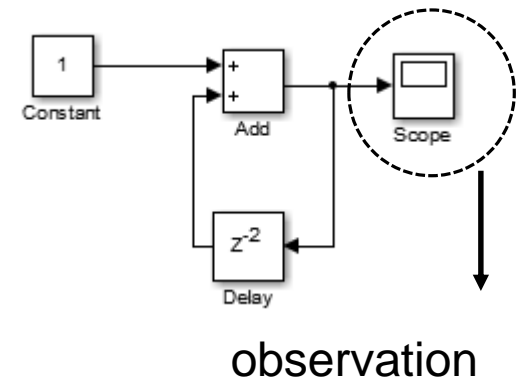
$$l_1(t) = -l_2(t), \frac{d}{dt} l_2(t) = l_1(t)$$

Equation holds for simulation step size $h \rightarrow 0$

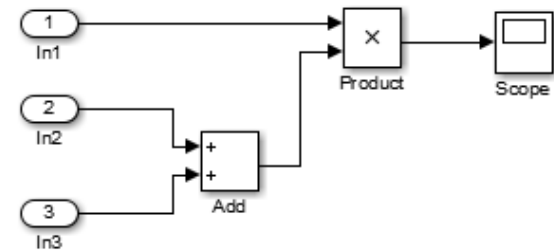
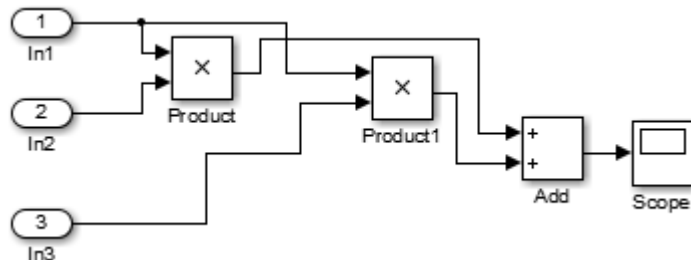
Adaptation of Approximate Bisimulation

- Simulink Model is graph $M = (B, V, I, O)$
- States $Q \subseteq \mathbb{R}^V$
- Observations $\Pi \subseteq \mathbb{R}^{\cup_{b \in O} \text{var}(b)}$
- Metric $d: \Pi \times \Pi \rightarrow \mathbb{R}$,

$$d(\langle \sigma_1 \rangle, \langle \sigma_2 \rangle) = \|\langle \sigma_1 \rangle - \langle \sigma_2 \rangle\|_\infty$$



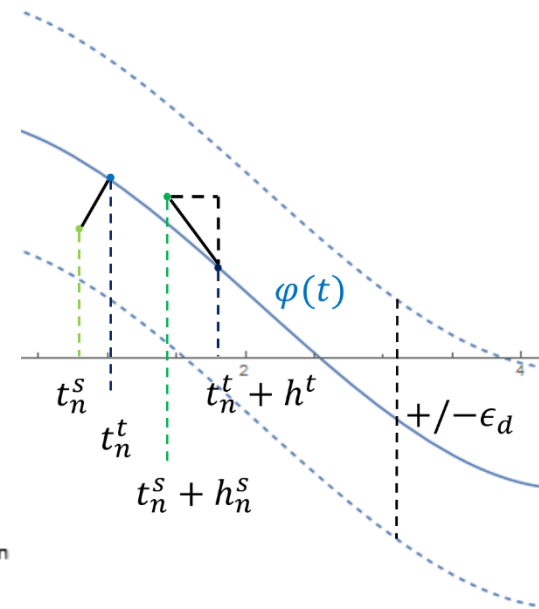
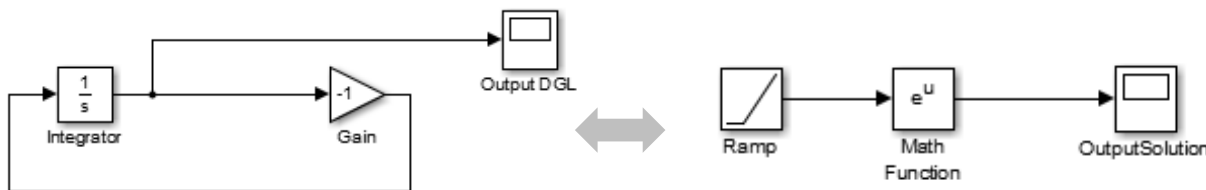
⇒ **Unsampled Models**: approx. bisimilar with $\epsilon = 0$



⇒ **Discrete Models:** approx. bisimilar with $\epsilon = 0$



⇒ **Continuous Models:** approx. bisimilar with ϵ depending on second derivative of solution (for Euler technique)



Summary

- Our goal: verification methodology of refactorings for hybrid Simulink models
- Ideas:
 1. abstract representation, sound with operational semantics
 2. adaptation of approximate bisimulation, allowing observations `close` to each other

Future Work

- Automation
- Support for hybrid models containing both, discrete and continuous parts
- Enhancement of estimation of epsilon tubes